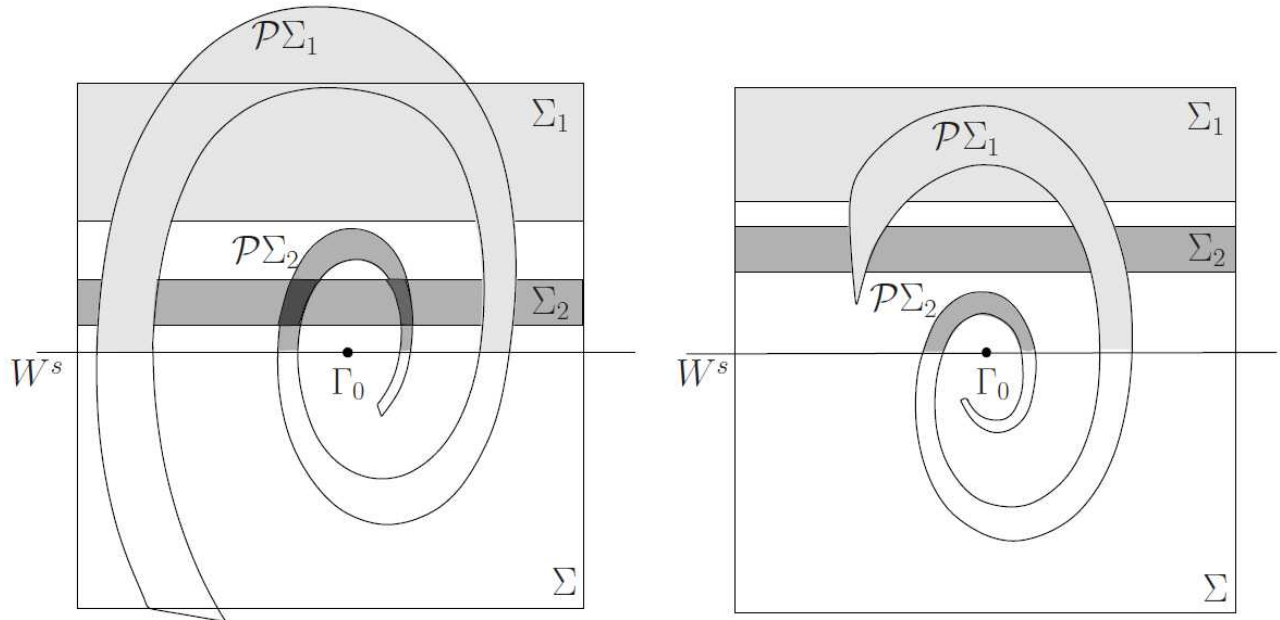
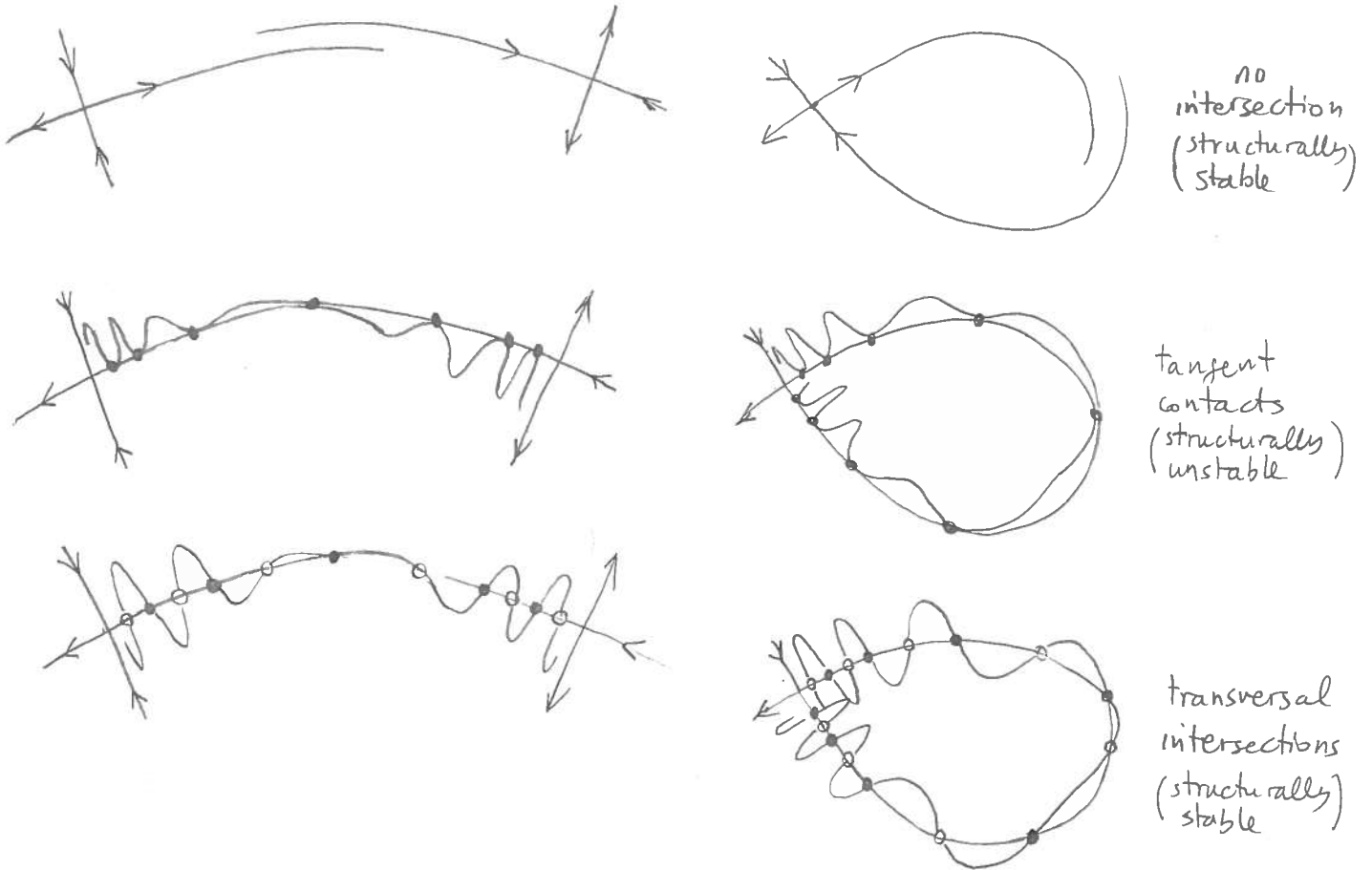


Figure 7.17: Construction of the Poincaré map \mathcal{P} in the saddle-focus case.



Homoclinic and heteroclinic connections and bifurcations
in d.t. (reversible) systems



Homoclinic/heteroclinic bifurcation: the tangent contact between a pair of homoclinic/heteroclinic connections

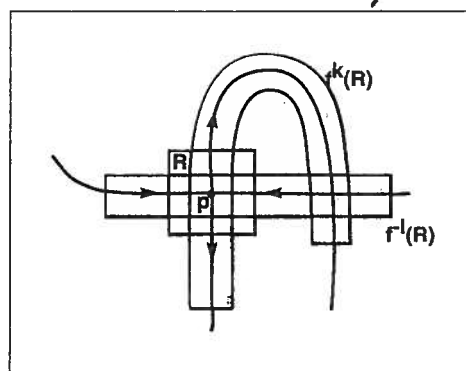
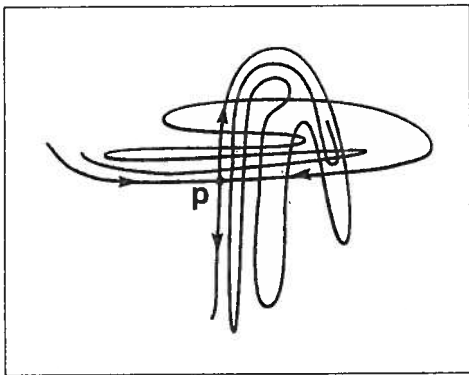


Figure 10.11 Construction of a horseshoe near a homoclinic point.
 The stable and unstable manifolds of a saddle p intersect in a homoclinic point x . A rectangle R is centered at p . Then for some positive integers k and l , k forward iterates of R and l backward iterates of R intersect at x , so that f^{k+l} forms a horseshoe.

Figure 10.10 Tangle of stable and unstable manifolds implied by homoclinic points.

If the stable and unstable manifolds of a fixed-point saddle or periodic point p cross in one homoclinic point, then they cross infinitely many times: each forward and backward iterate of a homoclinic point is a homoclinic point.